

A High Q Band Pass Filter Using Two Operational Amplifiers

*Seema Rana**, *Kapil Dev Sharma*** and *Kirat Pal****

*DAV Centenary Public School, Hardwar – INDIA

**Department of Physics , DAV(PG) College, Dehradun(Uttranchal) - INDIA

***Department of Earthquake Engineering

I. I. T. Roorkee – 247 667,INDIA

E-mail: kirat.pal@gmail.com

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ABSTRACT

A high Q band pass filter using two operational amplifiers is reported. The quality factor Q of the circuit is controllable through a single resistance. The results of experimental and theoretical studies are presented and confirms the theory.

1. Introduction

The application of band pass filter for selecting a band of frequencies is well known in the open literature. In general form the transfer function of a band pass filter is given by

$$T(s) = \frac{a_0 s}{a_1 + b_1 s + b_2 s^2} \quad (1)$$

where a_0 , a_1 , b_1 and b_2 are constants.

The quality factor Q of the band pass filter is governed by the term b_1 . It has infinite Q if b_1 approaches zero value but practically it is not possible although some high value up to $Q=20$ is easily possible.

In the literature number of circuits of band pass filter using operational amplifiers are available [1-5]. Here the new circuit of band-pass filter using only two operational amplifier is presented which has a controllable Q through a single resistance. The experimental results confirm the theory.

2. Circuit Description

Consider the general circuit shown in fig.1. Its voltage transfer function is given by

$$\frac{V_o}{V_i} = \frac{-Z_3 / Z_1}{\left(1 - \frac{Z_3 Z_4}{Z_5 Z_2}\right)} \quad (2)$$

if $Z_2 = Z_1$

$$\frac{V_o}{V_i} = \frac{-Z_3/Z_4}{\left(1 - \frac{Z_3 Z_4}{Z_1 Z_5}\right)} \quad (3)$$

put $Z_1 = \frac{1+sCR}{sC}$ combination of R in parallel with C

$Z_3 = \frac{R}{(1+sCR)}$ resistance R in series with C

$$Z_4 = R_4$$

$$Z_5 = R_5$$

and

Equation (3) becomes

$$\frac{V_o}{V_i} = \frac{sCR}{1 + s^2 C^2 R^2 + sCR(2-K)} \quad (4)$$

where $K = \frac{R_4}{R_5}$

The actual circuit is shown in fig.2.

The equation (4) represents a high Q band pass transfer function which is controllable through R_4 or R_5 . For sinusoidal input $s = j\omega$ the equation (4) becomes

$$\frac{V_o}{V_i} = -\frac{j\omega CR}{(1 - \omega^2 C^2 R^2 + j\omega CR(2-K))} \quad (5)$$

put $\omega CR = u$ (normalized form), equation(5) becomes

$$\frac{V_o}{V_i} = -\frac{ju}{(1 - u^2) + ju(2-K)} \quad (6)$$

Center frequency $u_0 = 1$, and gain $\left|\frac{V_o}{V_i}\right|$ is maximum at this value which is given by

$$\left|\frac{V_o}{V_i}\right|_{\max} = \frac{1}{2-K} \quad (7)$$

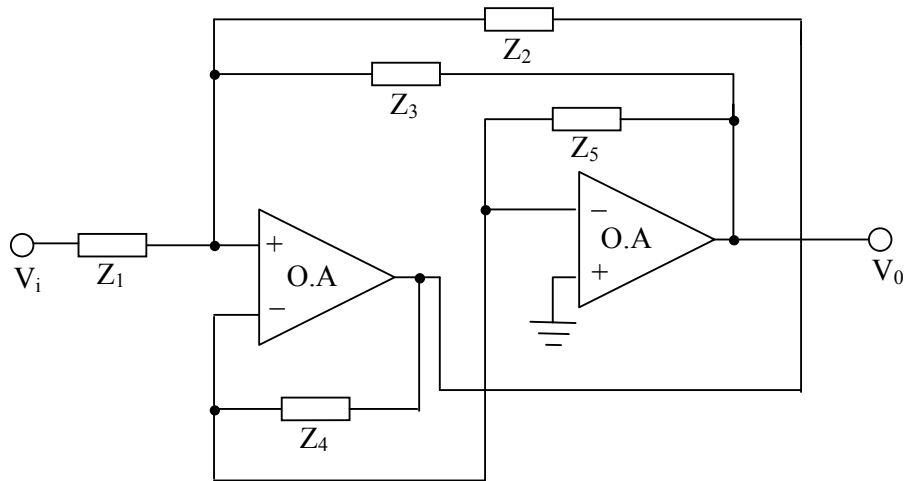


Fig.1. The General Circuit

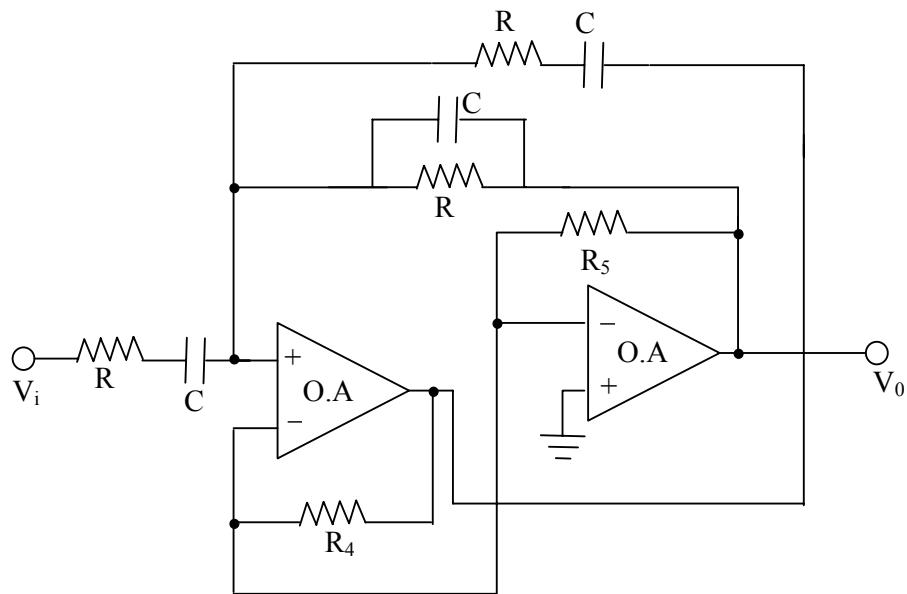


Fig.2. Actual Circuit of High Q Band Pass Filter

The lower and upper cutoff frequency u_1 and u_h occurs at $\frac{1}{\sqrt{2}}$ of maximum gain

i.e at $\frac{1}{\sqrt{2}} \times \frac{1}{(2-K)}$, and are given as

$$u_1 = \frac{-(2-K) + \sqrt{(2-K)^2 + 4}}{2} \quad (8)$$

$$u_h = \frac{(2-K) + \sqrt{(2-K)^2 + 4}}{2} \quad (9)$$

The bandwidth of the filter circuit is given by

$$\text{B.W.} = u_h - u_1$$

$$\text{Or B.W.} = (2-K) \quad (10)$$

$$\text{The quality factor } Q = \frac{u_o}{u_h - u_1}$$

$$\text{or } Q = \frac{1}{(2-K)} \quad (11)$$

It is clearly seen from eqn.(11) that Q approaches infinity as K approach the value 2.0. The Q can be controlled by R_4 or R_5 .

3. Experimental Results

The circuit was tested for $R=10K\Omega$, $C=0.001\mu F$, $R_5=10K\Omega$ and $R_4=15K\Omega$ in first experiment and for $R=10K\Omega$, $C=0.001\mu F$, $R_5=10K\Omega$ and $R_4=18K\Omega$ in second experiment. The IC 3140 which is an operational amplifier was used and operated with a $\pm 12V$ power supply. An input signal of 100mV was given in the frequency range of 1KHz to 100KHz. The results for $K=R_4/R_5=1.5$ and $K=1.8$ are shown in figure -3 and figure-4 respectively.

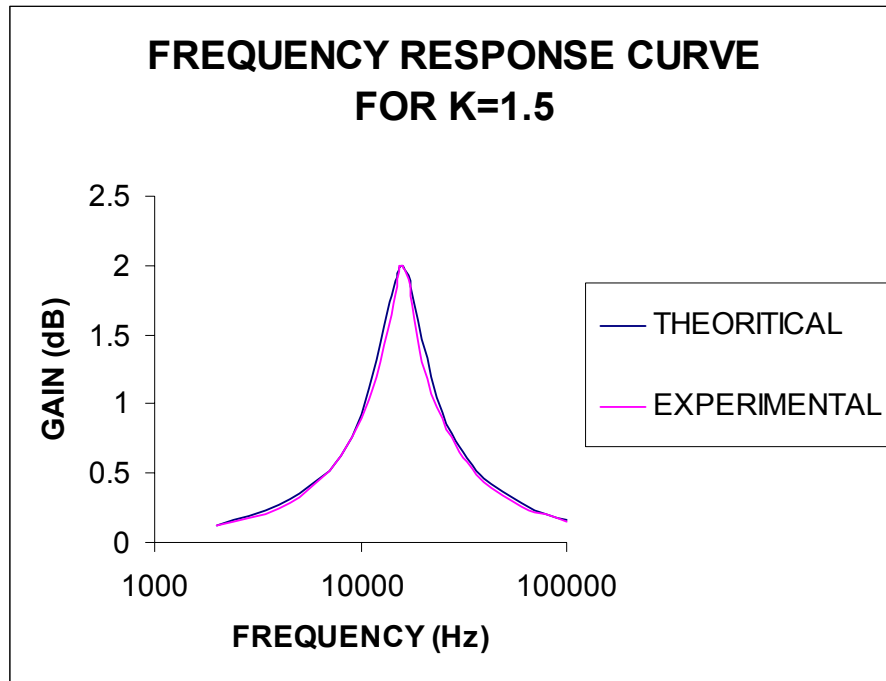


Fig.3. Frequency Response of Band Pass Filter (K=1.5)

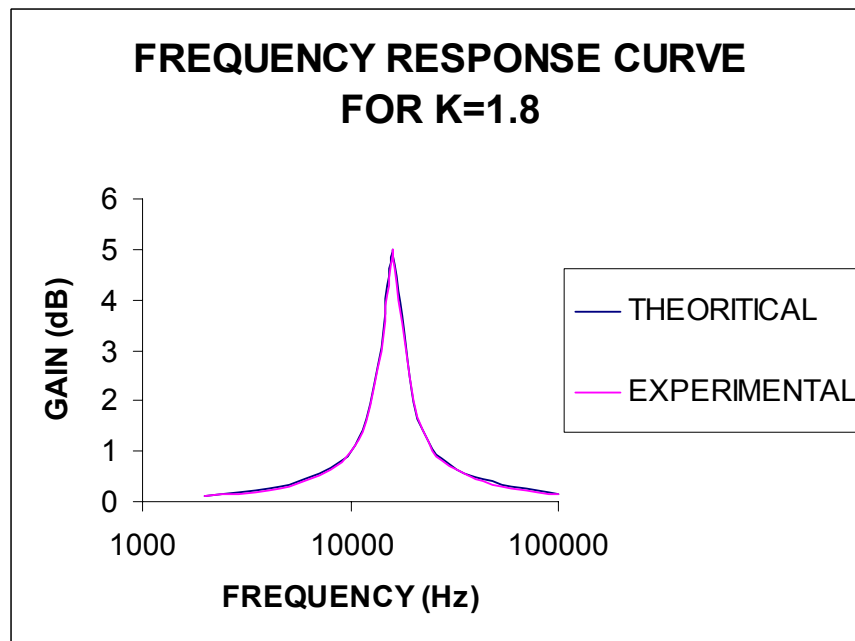


Fig.4. Frequency Response of Band Pass Filter (K=1.8)

4. Conclusions

A new type of band pass filter circuit has been reported. The circuit realises a high Q band pass filter, which is controllable through a single element as a resistance. The results of experimental study confirm the theoretical predictions made.

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