

**M.Sc. 3rd Semester Examination, 2023**

**APPLIED MATHEMATICS WITH  
OCEANOLOGY AND COMPUTER  
PROGRAMMING**

*( Discrete Mathematics )*

PAPER – MTM-304(New&Old)(CBCS)

*Full Marks : 50*

*Time : 2 hours*

*The figures in the right hand margin indicate marks*

*Candidates are required to give their answers in  
their own words as far as practicable*

1. Attempt any *four* questions out of *six* questions : 2 × 4
- (a) State De-Morgan's law for three variables.  
Using truth table, verify it.
- (b) What is Exclusive-OR Gate ?

*( Turn Over )*

- (c) Define the  $k$ -regular graph. Draw a 3-regular graph with 4 vertices.
- (d) Prove that the maximum number of edges in a connected simple graph with  $n$  vertices is  $n(n-1)/2$ .
- (e) Define the greatest element of a Poset with an example.
- (f) What is a semi-lattice? Give an example.
2. Attempt any *two* questions out of *six* questions : 4 × 4
- (a) Draw Karnaugh map and simplify the following Boolean expressions :
- (i)  $AB + A\bar{B} + \bar{A}\bar{B}$
- (ii)  $AB + A\bar{B}C + ABC$ .
- (b) Solve the recurrence relation of the Fibonacci numbers  $f_n = f_{n-1} + f_{n-2}$ ,  $n \geq 2$  with the initial conditions  $f_0 = 1, f_1 = 1$ , by the method of characteristic roots.

- (c) Draw a graph with 9 vertices having degree sequence 1,2,5,7,8,10.
- (d) Define bipartite graph and complete bipartite graph. Is a subgraph of a bipartite graph bipartite ?
- (e) Give the two definitions of lattice in connection with Poset and binary compositions, and show that they are equivalent.
- (f) Define sub-lattice with an example. Show that union of two sublattices is not a sublattice.

3. Attempt any *two* questions out of *four* questions : 8 × 2

- (a) (i) Write down the axioms of Boolean algebra. What are the main differences between Boolean algebra and algebra of real numbers.
- (ii) What is a Full Adder ? Write down the truth table and block diagram of it. Also, develop its logic circuit.

(b) Show that the maximum possible height of a strictly binary tree on  $2n + 1$  vertices is  $n$ .

(c) (i) Define finite-state machine with explanation.

(ii) Let  $M$  be the finite-state machine with state table appearing in the following :

(a) Find the input set  $\Sigma$ , the state set  $S$ , the output set  $O$ , and the initial state of  $M$ .

(b) Draw the state diagram of  $M$ .

(c) Find the output string for the input string  $aabbcc$ .

	$f$			$g$		
$S \backslash \Sigma$	$a$	$b$	$c$	$a$	$b$	$c$
$s_0$	$s_0$	$s_1$	$s_2$	0	1	0
$s_1$	$s_1$	$s_1$	$s_0$	1	1	1
$s_2$	$s_2$	$s_1$	$s_0$	1	0	0

- (d) (i) Using mathematical induction, prove that for any integer  $n > 1$ .

$$\frac{1}{1.2} + \frac{1}{2.3} + \dots + \frac{1}{n(n+1)} = \frac{n}{n+1}$$

- (ii) Define the cardinality of a set. What is the difference between relation and mapping? Explain all with examples.

**[ Internal Assessment – 10 Marks ]**

---