# M.Sc. 1st Semester Examination, 2023

## **CHEMISTRY**

PAPER-CEM-101

Full Marks: 50

Time: 2 hours

The figures in the right hand margin indicate marks

Candidates are required to give their answers in their own words as far as practicable

### GROUP - A

Answer any four questions from the following:

1. If  $\psi$  is a eigen function of an operator,  $\hat{A}$  with eigen value ' $\hat{a}$ ', then show that  $\psi$  is also an eigen function of  $e^{\hat{A}}$  with eigen value  $e^{a}$ .

- Spatial part of the ground state wavefunction of He atom is 1S (1) 1S(2).
  Write down the spin component of the above wave function.
- 3. Define a Grand Canonical Ensemble.
- 4. Write down the conditions at which the Fermi-Dirac distribution reduces to the Boltzmann distribution.
- 5. Give an example of each of the (i) Symmetric top and (ii) asymmetric top molecules.
- **6.** Evaluate the commutator,  $[\hat{p}_x, [\hat{x}, \hat{p}_x^2]]$ .

### GROUP - B

Answer any four questions from the following:

 $4 \times 4$ 

7. Write down the polar form of  $\hat{L}z$  operator. Deduce the normalized wavefunction of  $\hat{L}z$ 

1+3

- 8. For a particle in a box problem (x = 0 to L), evaluate  $\langle x^3 \rangle$  as  $x \to \infty$ .
- 9. Show that  $\beta = 1/kT$ , (where the symbols indicate their usual meaning) 4
- 10. How would you measure the acitivity of a volatile solute for practical system?
- 11. The rotational constant for H<sup>35</sup>Cl is observed to be 10.5909 cm<sup>-1</sup>. What are the values of B for H<sup>37</sup>Cl and <sup>2</sup>D<sup>35</sup>Cl?
- 12. State Virial theorem. For a conservative system, deduce the following relation,

$$\left\langle q_{i} \left( \frac{\partial v}{\partial q_{i}} \right) \right\rangle = 2T$$

(Symbols have their usual significances)

1 + 3

#### GROUP - C

Answer any **two** questions from the following:  $8 \times 2$ 

- 13. Wavefunctions for a rigid rotator are represented by the Spherical Harmonics functions,  $Y_i^m(\theta,\phi)$ ; where 'l' is the Azimuthal quantum number and 'm' is the magnetic quantum number. Show that  $-l \le m \le l$ .
- 14. Derive the Sackur-Tetrode equation for molar entropy of translational motion of a particle.What is the best composition of a mixture of a ternary system?
- 15. Derive an expression for the thermodynamic probability distribution of particles described by symmetric wave function and arrive at the appropriate quantum statistical distribution law.

16. What are the different advantages of Fourier transformation technology? What are hot bands? State (with justification) among the following molecules, whose rotational constant cannot be determined by spectroscopic method:

CH<sub>4</sub>, H<sub>2</sub>, CO<sub>2</sub>, HCl.

2 + 2 + 4

[Internal Assessment - 10 Marks]