

2022

1st Semester Examination

PHILOSOPHY

Paper : PHI 102

(Western Logic)

Full Marks : 40

Time : Two Hours

*The figures in the margin indicate full marks.  
Candidates are required to give their answers  
in their own words as far as practicable.*

Group - A

Answer any *four* out of the following questions :

5×4=20

1. State the rules for conjunction and rules for disjunction (with suitable examples) after the method of Resolution.

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2. Suppose A is True, B is False, X is False, Y is false, P and Q are unknown. Determine the truth value of the following sentences.

2½+2½

(a)  $(P \cdot \sim P. A) (P \vee Q \vee B)$ (b)  $[(A \cdot X) \supset Q] \equiv [A \supset (X \supset Q)]$ 

P.T.O.

3. (a) State the rules of inference of any two truth-functional connectives after Jeffrey's Truth Tree.  
 (b) Determine the validity of the following statement using Truth Tree.

$$A \leftrightarrow B, A \vee B / \therefore A \& B \quad 2+3$$

4. Write down two definite conventions governing the expressions ' $\Phi\mu$ ' and ' $\Phi\nu$ '. 2½+2½
5. Explain the final version of UG 5
6. Identify and explain the mistakes in the following erroneous proof.

$$1. (\exists x)(y)[Fx.Gx \supset Hy] / \therefore (\exists x)[(Fx.Gx) \supset Hx]$$

$$2. (y)[(Fz.Gz) \supset Hy]$$

$$3. (Fz.Gz) \supset Hy - 2, UI$$

$$4. (\exists x)[(Fx.Gz) \supset Hy] - 3, EG$$

$$5. (y)(\exists x)[(Fx.Gy) \supset Hy] - 4, UG$$

$$6. (y)(\exists x)[(Fx.Gy) \supset Hy] - 1, 2 - 5, EI$$

$$7. (\exists x)[(Fx.Gy) \supset Hy] - 6, UI \quad 2½+2½$$

### Group - B

Answer any *two* out of the following questions :

10×2=20

7. State and explain the *Reductio Ad Absurdum* Method in your own words. 10

8. (a) Determine whether the following argument is valid.

$$(A \vee B) \supset (A \cdot B), \sim (A \vee B) / \therefore \sim (A \cdot B)$$

- (b) Determine whether the following statements are equivalent.

(i)  $(P \supset Q) \supset R, P \supset (Q \supset R)$

(ii)  $(A \cdot B) \vee (A \cdot C) \vee (B \cdot C), (A \vee B) \cdot (A \vee C) \cdot (B \vee C)$  4+(3+3)

9. (a) What is validity?

- (b) Prove the validity of the following :

(i) 1.  $(\exists x)Xx \supset (y)(Yy \supset Zy) /$

$$\therefore (\exists x)(Xx \cdot Yx) \supset (\exists y)(Xy \cdot Zy)$$

(ii) 1.  $(x)(\exists y)(Kx \cdot Ly) / (\exists y)(x)(Kx \cdot Ly)$

2+(4+4)

10. (a) What is invalidity?

- (b) Prove the invalidity of the following :

(i) 1.  $(x)(\exists y)(Ex \supset Fy)$

2.  $(\exists y)(z)(Fy \supset \sim Gz) / \therefore (x)(z)(Ex \supset \sim Gz)$

(ii) 1.  $(\exists x)(\exists y)(Yx \supset Zy)$

2.  $(\exists y)(z)(Zy \supset Az) / \therefore (\exists x)Yx \supset (z)Az$

2+(4+4)