Appendix A

Coupled differential equations of the time dependent coefficients corresponds to different field modes are

$$\dot{A}_{1} + i\omega_{c}A_{1} = 0$$

$$\dot{A}_{2} + i\omega_{c}A_{2} + igA_{1}B_{1}^{*2} = 0$$

$$\dot{A}_{3} + i\omega_{c}A_{3} + igA_{1}B_{1}^{2} = 0$$

$$\dot{A}_{4} + i\omega_{c}A_{4} + 2igA_{1} = 0$$

$$\dot{A}_{5} + i\omega_{c}A_{5} + igA_{1} = 0$$

$$\dot{B}_{1} + i\omega_{m}B_{1} = 0$$

$$\dot{B}_{2} + i\omega_{m}B_{2} + 2igB_{1} = 0$$

$$\dot{B}_{3} + i\omega_{m}B_{3} + 2igB_{1}^{*} = 0$$