

012

MCA

3<sup>rd</sup> SEMESTER EXAMINATION

THEORY OF FORMAL LANGUAGE AND AUTOMATA

PAPER—MCA-302

Full Marks : 100

Time : 3 Hours

*The figures in the margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable.**Illustrate the answers wherever necessary.*

Answer any five questions.

5×14

1. (a) Define a Mealy machine with suitable example. 3
- (b) Construct a Mealy machine equivalent to the Moore machine defined by the following table : 5

Present State	Next State		Output
	a = 0	a = 1	
→ q <sub>0</sub>	q <sub>3</sub>	q <sub>1</sub>	0
q <sub>1</sub>	q <sub>1</sub>	q <sub>2</sub>	1
q <sub>2</sub>	q <sub>2</sub>	q <sub>3</sub>	0
q <sub>3</sub>	q <sub>3</sub>	q <sub>0</sub>	1

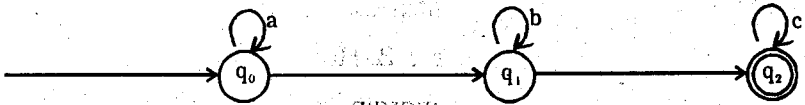
(Turn Over)

(c) Find the DFA which accepts all strings over  $\{a, b\}$  terminating by the substring  $ba$ . 6

2. (a) Find a grammar generating  $\{a^j b^n c^n \mid n \geq 1, j \geq 0\}$  6

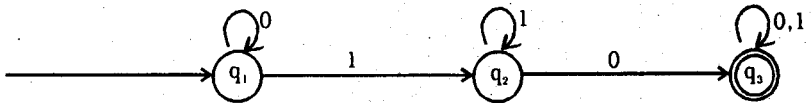
(b) What do you mean by monotonic grammar? Give examples.

(c) Consider transition system, containing  $\wedge$  move.



Obtain an equivalent transition system without  $\wedge$  move. 5

3. (a) Describe the set accepted by the finite automaton where transition diagram is shown below : 7



(b) State and prove Arden's theorem. 1+3

(c) Construct the finite automaton equivalent to the regular expression : 3

$$0^* (00 + 11) 1^*$$

4. (a) Define ambiguous grammar, explain with example. 4
- (b) Design CFG for the set of all strings which are palindromes over an alphabet set  $\Sigma = \{a, b\}$ . 5
- (c) Find an equivalent CNF for the given

$$G = (\{S, A, B, D\}, \{a, b\}, P, S)$$

where productions are

$$S \rightarrow a^A D$$

$$A \rightarrow a^B / b^A B$$

$$B \rightarrow b$$

$$D \rightarrow$$

5. (a) Find a reduced grammar equivalent to the grammar :  
 $S \rightarrow aAa, A \rightarrow bBB, B \rightarrow ab \mid D, C \rightarrow aB, D \rightarrow EE \mid ab.$  7
- (b) Construct a grammar in Greibach normal from equivalent to the grammar : 7

$$S \rightarrow AA \mid a, A \rightarrow SS \mid b.$$

6. (a) Prove that the family of context free language is closed under union but not closed under intersection. 6+3
- (b) Construct a NPDA for the language : 6  
 $L = \{w \in \{a, b\}^* : n_a(w) = n_b(w)\}$

7. (a) Construct a PDA accepting the following Language : 7  
 $L = \{wcw^T \mid w \in \{a, b\}^*\}$
- (b) Construct a PDA A equivalent to the following context free grammar :

$$S \rightarrow 0BB$$

$$B \rightarrow 0S \mid 1S \mid 0$$

Test whether 1011010 is in  $N(A)$ .

4+3

8. (a) Design a Turing Machine over  $\{1, b\}$  which can compute a concatenation function over  $\Sigma = \{1\}$ . If a pair of words  $(w_1, w_2)$  is the input, the output has to be  $w_1w_2$ . 7

(b) Construct a Turing Machine that can accept the strings over  $\{0, 1\}$  containing even number of 1's. 7

**Internal Assessment**

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**30**