

**2019**

**MSc**

**2<sup>nd</sup> Semester Examination**

**APPLIED MATHEMATICS WITH OCEANOLOGY AND  
COMPUTER PROGRAMMING**

**PAPER – MTM-202**

**Full Marks : 50**

**Time : 2 Hours**

The figures in the right-hand margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

Illustrate the answers wherever necessary.

## (Numerical Analysis)

1. Answer any **FOUR** questions:

(2x4)

- Compare Newton-Cote's quadrature and Gaussian quadrature.
- The iterative methods are better than direct methods to solve a system of linear equations. Explain.
- Write the sufficient conditions for the convergence of Newton-Raphson method to solve a system of nonlinear equations containing two variables and three variables.
- What are the advantages to approximate a function using orthogonal polynomials?
- Write down the steps to evaluate  $\int_a^b f(x)dx$  by Monte-Carlo method.
- Is the following function a cubic spline? Justify.

$$P(x) = \begin{cases} x^3 - 4x^2 + 5x - 2, & 1 \leq x \leq 3 \\ x^3 + x^2 + 25x + 43, & 3 \leq x \leq 4 \end{cases}$$

- Write down the expressions of zeros of the chebyshev polynomial of degree n.
- What does mean by absolute and relative stable of

$$\frac{dy}{dt} = \lambda y, \quad y(0) = y_0$$

2. Answer any **FOUR** questions:

4x4

- Discuss Gauss-Jordan method to find the inverse of a square matrix by partial pivoting method.
- Explain a suitable method to solve a system of tri-diagonal linear equation.
- Find the least squares solution of the system of equations  $x + y = 3.0$ ;  $2x - y = 0.03$ ,  $x + 3y = 7.03$  and  $3x + y = 4.97$ .
- Define Chebyshev polynomial. Show that it is even under certain conditions to be stated by you. Express  $x^4$  in terms of Chebyshev polynomials.
- Describe approximation of a continuous function using orthogonal polynomials.
- Evaluate the value of the integration  $\int_1^2 \frac{1}{1+x} dx$  by Gauss Legendre four points quadrature formula.

g) Discuss the stability of Euler's method of the ODE  $\frac{dy}{dt} = \lambda y$ ,  $y(0) = y_0$ .

h) Solve the following BVP,  $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = 10x$  with boundary conditions  $y(0)=0$  and  $y(1)=0$ , at the points  $x=0.25, 0.50, 0.75$ .

3. Answer any **TWO** questions:

8x2

- a) Describe LU-decomposition method to solve a system of linear equations. 8  
 b) Describe an implicit method to solve the following equation:

$$\frac{\partial u}{\partial t} = \alpha \frac{\partial^2 u}{\partial x^2}$$

Subject to the boundary conditions  $u(0,t) = f_1(t)$ ,  $u(1,t) = f_2(t)$  and initial condition  $u(x,0) = g(x)$  8

- c) Find all the eigen values and corresponding eigen vectors of the symmetric 8  
 matrix  $\begin{pmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{pmatrix}$  using Jacobi's method.

- d) What do you mean by spline interpolation. Describe natural cubic spline 1+7  
 interpolation.

[ Internal Assessment: 10 Marks ]