

2018

PHYSICS

[Honours]

PAPER – IV

Full Marks : 90

Time : 4 hours

*The figures in the right hand margin indicate marks
Candidates are required to give their answers in their
own words as far as practicable*

Illustrate the answers wherever necessary

[NEW SYLLABUS]

GROUP—A

Answer any two questions 15 × 2

1. (a) State D'Alembert's principle. Establish Lagranges' equation from D' Alembert's principle for a conservative, holonomic system. 1 + 5

(Turn Over)

(2)

(b) Two particles A and B having masses m_1 and m_2 respectively are moving in a two dimensional plane such that the distance between them remains constant.

(i) What is the number of degrees of freedom ?

(ii) Find the co-ordinates of centre of mass and the reduced mass.

(iii) Choose an appropriate set of generalised co-ordinates describing the dynamics of two particle system.

(iv) Set up Lagrange's equations of motion for these co-ordinates in absence of any applied field.

(v) Obtain solutions of these equation.

(vi) Give physical interpretation of each solution.

$1 + 2 + 1 + 2 + 2 + 1$

2. (a) What are the essential features of vector atom model.

2

- (b) Explain, with a neat diagram, the doublet structure of Sodium lines. 3
- (c) Explain LS coupling scheme for addition of angular momenta. What is jj coupling ? Why is it applicable only to heavy elements. 2 + 1 + 1
- (d) What are Stokes and antistokes lines in Raman effect ? 2
- (e) Why are the anti-stokes lines less intense than stokes line. The exciting line in an experiment is 5460Å and that the stokes line is at 5520Å. Find the wavelength of the antistokes line. 2 + 2
3. (a) Draw the circuit diagram of Wien-Bridge oscillator with OPAMP as an active element. Explain its operation. 2 + 4
- (b) A Wien Bridge Oscillator is used for a frequency range 30 Hz to 3kHz. The variable capacitance has a range 50pF to 5000 pF.

(4)

Find out the resistance values required.
If the resistance in the other arms are in the
ratio 5 : 1, find out the gain of the amplifier.
Deduce any formula used. 2 + 3

(c) Design a 4 bit shift register using *D* flip-flops
and explain its operation. 2 + 2

4. (a) What are the process through which γ -ray
interact with matter ? 3

(b) Explain the nature and origin of β ray
spectrum. 2 + 2

(c) Explain how the conservation laws are hold
in case of β -decay. 3

(d) Explain qualitatively that emission of *k* shell
electron is more probable during photo-
electric emission by γ -ray. 3

(e) Calculate the minimum energy required for
pair-production. 2

GROUP -B

Answer any five questions :

8 × 5

5. (a) What are the advantages of using negative feedback over positive feedback in case of amplifier? 2
- (b) Draw a circuit diagram of a two stage RC coupled transistor amplifier and find the expression for mid frequency voltage gain. 1 + 2
- (c) The mid band voltage gain of an RC coupled amplifier is 150. At frequencies of 100 Hz and 100 kHz, the gain fall to 75. Determine bandwidth. 3
6. (a) Derive the Euler's equation of motion for an ideal fluid. Hence derive Bernoulli's equation. 2 + 3
- (b) Find whether given \vec{V} (Velocity) is a possible motion for an incompressible ideal fluid. 3

$$\vec{v} = -\frac{2xyz}{(x^2 + y^2)} \hat{i} + \frac{(x^2 - y^2)z}{(x^2 + y^2)} \hat{j} + \frac{yz^2}{x^2 + y^2} \hat{k}$$

7. (a) Using Hamilton's Canonical equations, derive the equation of motion of a particle moving in a force field in which the potential is given by

$$V = -\frac{k}{r} ; \text{ where } k \text{ is a positive constant.}$$

Explain, whether energy and angular momentum is conserved or not in this motion. 3 + 2

- (b) Define cyclic or ignorable co-ordinates. Show that the generalised momenta corresponding to cyclic co-ordinates are conserved. 1 + 2

8. (a) What is nuclear isomerism? Explain with example. 2
- (b) Describe Gamow's theory for decay of α particle from radioactive nuclei. 3
- (c) What do you mean by fine structure of α -particle? 3

9. (a) State the semi empirical mass formula for nuclear binding energy. 3
- (b) What is Mass parabola ? How does mass parabola explain the stability of nuclei of same isobar. 1 + 2
- (c) What is the value of electric quadrupole moment of $^{208}_{82}\text{Pb}$? 1
- (d) Why $^{17}_8\text{O}$ is spontaneous neutron emitter when excited by preceding β -decay ? 1
10. (a) Explain the difference between the spontaneous and the stimulated emissions. 3
- (b) What do you mean by Enistein's A, B coefficients ? Show that the ratio

$$\frac{A}{B} = \frac{8\pi h\nu^3}{c^3}$$

where the symbols used having their usual significance. 1 + 3

- (c) Find the value of Lande g -factor for S -state. 1
11. (a) For the electronic transition ${}^1D_2 \rightarrow {}^1P_2$
- (i) Draw the energy level diagram and show Zeeman splitting of the energy levels in the presence of a magnetic field.
 - (ii) Show allowed transitions
 - (iii) How many distinct lines are obtained in the Zeeman Spectrum. $(2 + 2) + 2 + 1$
- (b) State Moseley's law of X-ray. 1
12. (a) What are the differences between combinational logic and sequential logic? 2
- (b) Design a 4 to 1 multiplexer using basic gates. 2
- (c) "FET is a voltage controlled device whereas BJT is a current controlled device explain. 2
- (d) Draw the transfer characteristic curve of an n -channel JFET and explain the nature of curve. 2

GROUP - C

Answer any five questions : 4 × 5

13. Two masses m_1 and m_2 rest on a smooth surface. A spring of negligible mass and spring constant k and of length l_0 at rest joins the masses. Assuming the motion to remain one dimensional calculate (i) the normal frequency and (ii) normal co-ordinate. 2 + 2

14. Show that

$$Q = \log \left(\frac{1}{q} \sin p \right)$$

and $p = q \cot p$ is a canonical transformation. Find the generating function. 2 + 2

15. Prove that if the dynamical variables f and g are constant of motion, then their Poisson Bracket is also a constant of motion. 4

16. (a) What is continuous and characteristics X-ray spectrum.
- (b) Find the critical voltage that must be applied to an X-ray tube to excite the k -series of copper. Given that k -absorption limit is 1.38A. 2 + 2
17. What are tuned amplifiers? What are their practical uses? Draw the circuit diagram of a single tuned RF transistor amplifier. Draw the nature of its frequency response curve. 1 + 1 + 1 + 1
18. (a) Draw an inverter circuit using MOSFET.
- (b) Draw a single bit digital comparator using basic gates. 2 + 2
19. A radioactive sample has its half-life equal to 60 days. Calculate its
- (i) disintegration constant
- (ii) average life
- (iii) time for $\frac{1}{4}$ of the original number of atoms to remain unchanged. 1 + 1 + 2

20. Suppose a sinusoidal signal $V_s = 10 \sin 2000 \pi t$ is applied to the input of the given OP-AMP circuit with $R = 1 \text{ M}\Omega$ and $C = 1 \mu\text{F}$. Find the output voltage and draw its waveform. 4

