2015

M.Sc.

3rd Semester Examination APPLIED MATHEMATICS WITH OCEANOLOGY AND COMPUTER PROGRAMMING

PAPER-MTM-306(U-II)

(PRACTICAL)

Full Marks: 25

Time: 2 Hours

The figures in the right-hand margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

Illustrate the answers wherever necessary.

(Advanced Numerical and Statistical Techniques : Using C/C++/MATLAB)

Answer any one question.

Problem: 16 marks; Lab. Note Book and Viva: 4+5 marks

(Question will be selected by lottery.)

1. Write a program to solve the equation by Runge-Kutta (2nd and 4th order) methods:

$$\frac{dy}{dx} = 5x + 5y^2$$
, y(0) = 1,

find y in the interval $0 \le x \le 0.5$, taking h = 0.1.

2. Write a program to solve the following pair of first order first degree ODEs by 4th order Runge-Kutta method:

$$\frac{dy}{dx} = -2y + 3z, \quad \frac{dz}{dx} = y + 9z$$

with y(0) = 6, z(0) = 4 for x = 0.1, 0.2.

3. Write a program to find the following integration by Gauss-Legendre quadrature (6-point) formula:

$$\int_{0}^{2} \left(e^{x} + \log \left(2x + 1 \right) \right) dx.$$

4. Write a program to solve the equation:

$$\frac{dy}{dx} = 2x^2 + 5y$$
, $y(0) = 2$ $0.1 \le x \le 0.5$

by Euler's method taking h = 0.1.

- 5. Write a program to find the regression lines for a bivariate sample.
- 6. Write a program to fit a linear curve for a bivariate sample.
- 7. Write a program to fit a quadratic curve for a bivariate sample.
- 8. Write a program to find the inverse of a matrix by partial pivoting. Use this program to solve a system of linear equations.
- 9. Write a program to solve a system of linear equations by Gauss elimination method.
- 10. Write a program to evaluate a determinant by Gauss elimination method, using partial pivoting.

11. Write a program to solve the following ODE by Milne predictor-corrector methods for x = 0.4, 0.5, 0.6:

$$\frac{dy}{dx} = x^2 + 2y$$
, $y(0) = 1$.

- 12. Write a program to find the correlation coefficient for a bivariate sample.
- 13. Write a program to solve a system of tri-diagonal equations.
- 14. Write a program to find the largest Eigenvalue of a square matrix by power method.
- 15. Write a program to find the multiple correlation coefficient for the sample (x_i, y_i, z_i) , i = 1, 2, ..., n.
- 16. Write a program to find two partial correlation coefficients for the sample (x_i, y_i, z_i) , i = 1, 2, ..., n.
- 17. Write a program to solve a system of linear equations by Gauss Seidal iteration method.
- 18. Write a program to solve a system of linear equations by LU decomposition method.