

**NEW****2015****BCA****4th Semester Examination****OPERATIONS RESEARCH****PAPER—2203***Full Marks : 100**Time : 3 Hours**The figures in the right-hand margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable.**Illustrate the answers wherever necessary.*

Answer any seven questions.

1. Solve the following L.P.P. by Simplex method :

$$\text{Maximize } Z = 3x_1 + 2x_2$$

$$\text{Subject to : } x_1 + x_2 \leq 4$$

$$x_1 - x_2 \leq 2$$

$$x_1, x_2 \geq 0.$$

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2. Use penalty (Big-M) method, solve the following L.P.P. :

$$\text{Maximize } Z = 3x_1 - x_2$$

$$\text{Subject to : } 2x_1 + x_2 \geq 2$$

$$x_1 + 3x_2 \leq 3$$

$$x_2 \leq 4$$

$$x_1, x_2 \geq 0.$$

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3. Solve the problem by two-phase method :

$$\text{Minimize } Z = x_1 + x_2$$

$$\text{Subject to : } 2x_1 + x_2 \geq 4$$

$$x_1 + 7x_2 \geq 7$$

$$x_1, x_2 \geq 0.$$

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4. Prove that dual of the dual of a given primal is the primal.

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5. Apply the principle of duality to solve the LP problem :

$$\text{Maximize } Z = 3x_1 - 2x_2$$

$$\text{Subject to : } x_1 + x_2 \leq 5$$

$$x_1 \leq 4$$

$$1 \leq x_2 \leq 6$$

$$x_1, x_2 \geq 0.$$

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6. Solve the following problem by dual simplex method :

$$\text{Minimize } Z = 2x_1 + x_2$$

$$\text{Subject to : } 3x_1 + x_2 \geq 3$$

$$4x_1 + 3x_2 \geq 6$$

$$x_1 + 2x_2 \geq 3$$

$$x_1, x_2 \geq 0.$$

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7. Solve the following transportation problem using Vogel's Approximation Method (VAM) :

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	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	a <sub>i</sub>
O <sub>1</sub>	10	7	3	6	3
O <sub>2</sub>	1	6	8	3	5
O <sub>3</sub>	7	4	5	3	7
b <sub>j</sub>	3	2	6	4	

8. Find the optimal assignments to find the minimum costs for the assignment problem with the following Cost matrix :

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	I	II	III	IV	V
A	6	5	8	11	16
B	1	13	16	1	10
C	16	11	8	8	8
D	9	14	12	10	16
E	10	13	11	8	16

9. Solve the following game problem using dominance principle : 10

		<i>Player B</i>				
		I	II	III	IV	V
<i>Player A</i>	I	3	5	4	9	6
	II	5	6	3	7	8
	III	8	7	9	8	7
	IV	4	2	8	5	3

10. The following table lists the jobs of a network along with their time estimates :

Job (i→j)	Time duration (days)		
	<i>Optimistic (a)</i>	<i>Most likely (m)</i>	<i>Pessimistic (b)</i>
1 → 2	3	6	15
1 → 6	2	5	14
2 → 3	6	12	30
2 → 4	2	5	8
3 → 5	5	11	17
4 → 5	3	6	15
6 → 7	3	9	27
5 → 8	1	4	7
7 → 8	4	19	28

Draw the project network and calculate the length and variance of the critical path. 10

**[Internal Assessment — 30]**