

2016

PHYSICS

[Honours]

PAPER – I

Full Marks : 90

Time : 4 hours

*The figures in the right hand margin indicate marks
Candidates are required to give their answers in their
own words as far as practicable*

Illustrate the answers wherever necessary

[NEW SYLLABUS]

GROUP – A

Answer any two questions : 15×2

1. (a) Expand the following function in Taylor series $F(z) = \log_e(1+z)$ around $z = 0$. 3

(Turn Over)

- (b) What is the geometrical interpretation of 'divergence'? State Gauss's divergence theorem. Find the divergence of the function

$$\vec{V} = r(2 + \sin^2 \phi) \hat{r} + r \sin \phi \cos \phi \hat{\phi} + 3z^2 \hat{z}$$

where \hat{r} , $\hat{\phi}$, \hat{z} represent the unit vectors in cylindrical co-ordinate.

1 + 1 + 3

- (c) Find the integral

$$\int_{-1}^{+1} x^2 P_n(x) P_m(x) dx$$

where $P_n(x)$ represent Legendre polynomial of degree n .

3

- (d) Expand in a Fourier series the periodic function $f(x)$ with period $2l$ where

$$f(x) = |x| \text{ for } -l < x < l$$

Hence show that

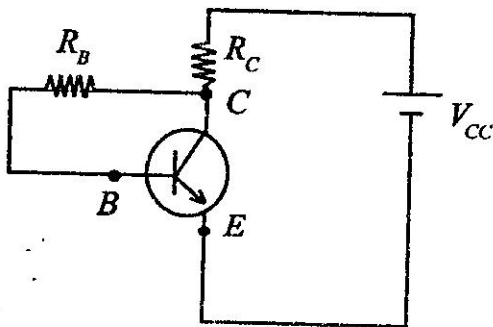
$$\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8} \quad 3 + 1$$

2. (a) Find the expression for the steady state displacement of a particle serving as a linear

harmonic oscillator under the action of an external periodic force $F \cos \omega t$. Find the instantaneous velocity of the particle and show that the velocity and the displacement differ in phase by $\pi/2$. 2 + 2 + 1

- (b) What do you mean by velocity resonance? Plot the variation of velocity amplitude of the forcing system against angular frequency of the driving force for different values of decay constant? How does sharpness of resonance changes with decay constant? 1 + 1 + 1
- (c) What do you mean by acoustic pressure and acoustic intensity? Show that the acoustic intensity for a plane progressive harmonic wave is the product of the rms acoustic pressure and rms particle velocity. 1 + 1 + 2
- (d) The intensity level in a conversation is 70 dB above the threshold of 10^{-12} W/m^2 . Calculate the amplitude of vibration of the air particles in the sound wave. Given velocity of sound = 350 m/s, density of air = 1.25 g/litre mean frequency = 500 Hz. 3

3. (a) What do you mean by reverse saturation current? On which factors does it depend? 1+1
- (b) What do you mean by the stability of bias point of a transistor? Find the stability factor of a voltage divider type transistor biasing circuit using emitter resistance. Find the condition for its optimum operation. 1+3+1
- (c) Consider the following circuit :



Here $V_{CC} = 12 \text{ V}$, $R_C = 1 \text{ k}\Omega$, $\beta = 100$, and $V_{BE} = 0.7 \text{ V}$. Find R_B which makes $V_{CE} = 6.32 \text{ V}$, Find also I_B . Assume $I_{CBO} \ll I_B$. 3

(d) Show that

$$(A \oplus B) \oplus C = A \oplus (B \oplus C)$$

symbols have their usual meaning.

2

(e) Show that a shear θ is equivalent to two equal linear tensile strains of half the magnitude in mutually perpendicular direction.

3

4. (a) Explain the terms "spatial coherence" and "temporal coherence" with reference to Young's double slit experiment for interference pattern.

 $1\frac{1}{2} + 1\frac{1}{2}$

(b) Show that the shape of the fringes produced in Young's experiment is hyperbolic in two dimensional plane.

4

(c) When a film of transparent material of refractive index 1.2 is put behind one of the slits of a two-slit Young's experiment, the zeroth order fringe moves to the position previously (before insertion of the film)

occupied by the 4th-order bright fringe. Given that the wavelength λ of the light used is 5000 Å, find the thickness of the film. 4

- (d) What do you mean by fringes of equal width and fringes of equal inclination? 2 + 2

GROUP – B

Answer any five questions : 8 × 5

5. (a) Define resolving power of a grating. Find an expression for the chromatic resolving power of a grating. 1 + 3
- (b) For sodium light (D lines – 589.0 nm and 589.6 nm) incident normally on a grating having 100 lines/mm of width 2 cm, calculate the first order
- (i) angle of diffraction
 - (ii) chromatic dispersion
 - (iii) resolving power.
 - (iv) Are the D lines resolved in the first order? (1 + 1 + 1 + 1)

6. (a) What do you mean by elliptically polarised light? Explain how a quarter-wave plate can be used to analyse polarised light. How can you distinguish between an elliptically polarised light and a mixture of plane polarised and unpolarised light? 1+3+2
- (b) What is zone plate? Explain its difference with convex lens. 1+1
7. (a) For stationary waves in a stretched transversely vibrating string, the displacement at a point x at a time t is

$$y(x,t) = \sum_{S=1}^{\infty} \frac{A}{S^2} \sin \frac{S\pi a}{L} \sin \frac{S\pi x}{L} \cos \frac{S\pi ct}{L}$$

where $x = a$ is the point of excitation and C is the velocity of propagation of the wave along the string. The other symbols are standard.

- (i) Find the initial displacement of the fifth harmonic.
- (ii) Calculate the frequency and the wavelength of second harmonic ($a \neq L/2$).

(iii) The string is excited at $x = a = L/3$.
Find the first three harmonics that are present.

(iv) What happens if the string after excitation be touched at the same point ($x = a$) ? 1+2+2+1

(b) Define 'decibel' and 'phon'. 2

8. (a) Set up the equation of motion of a spherical body of radius r moving vertically downward through a viscous fluid. Calculate the steady terminal velocity V_t . Draw V_t against r curve. 1 + 2 + 1

(b) Draw the circuit diagram of a Bridge rectifier. Explain its operation. 2 + 2

9. (a) What is resonance ? Distinguish between amplitude and velocity resonance. 1 + 3

(b) A plane progressive wave in one-dimension is given by $y = a \sin (wt - kx + \alpha)$ where the

notations have their usual meaning. Calculate the instantaneous kinetic energy and potential energy per unit volume for the wave.

4

10. Derive the system matrix for a combination of two thin lenses separated by a distance. Hence find the equivalent focal length. Find the positions of principal planes and discuss how the locations of principal planes change as a function of the distance between the two lenses.

3 + 1 + 4

11. (a) Draw the circuit diagrams for positive logic two input OR and AND gates using diodes and explain their operations.

2 + 2

(b) Establish the relation $I_C = \beta I_B + (1 + \beta) I_{CBO}$, where the symbols have their usual meanings.

2

(c) Subtract $(1101)_2$ from $(1010)_2$ by 1's complement method.

2

12. (a) Using Leibnitz's theorem derive Rodrigue's formula of Legendre polynomial.

5

(b) Show that (i) in polar co-ordinates

$$\frac{\partial(x,y)}{\partial(r,\theta)} = r \quad \text{(ii) in cylindrical co-ordinates}$$

$$\frac{\partial(x,y,z)}{\partial(\rho,\phi,z)} = \rho. \quad 3$$

GROUP - C

Answer any five questions : 4 x 5

13. Solve

$$x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} + 2y = x \log x \quad 4$$

14. Show that

$$\nabla^2(\log r) = \frac{1}{r^2} \quad 4$$

15. Distinguish between avalanche breakdown and Zener breakdown. 2 + 2

16. What is piezoelectricity ? Indicate briefly how is it used to generate ultrasonic waves. 2 + 2

17. Check Stoke's theorem for the vector

$$\vec{V} = (2xz + 3y^2)\hat{j} + (4yz^2)\hat{k}$$

for the surface of a unit square located at first quadrant of $Y-Z$ plane. 4

18. The equations of motion of two coupled oscillators are

$$\ddot{q}_1 + \sqrt{2}q_2 + 4q_1 = 0$$

and
$$\ddot{q}_2 + \sqrt{2}q_1 + 5q_2 = 0$$

Find the normal frequencies and the ratios of the amplitudes of the normal modes. 2 + 2

19. Newton's ring are formed with a source of light containing two wavelengths λ_1 and λ_2 . If m th order dark ring due to λ_1 coincides with the $(m + 1)$ th order dark ring due to λ_2 , Prove that the radius of the m th dark ring of λ_1 is equal to

$$\sqrt{\frac{\lambda_1 \lambda_2 R}{\lambda_1 - \lambda_2}}, \text{ where } R \text{ is the radius of curvature of lower curved surface. 4}$$