

2017**M.Sc. 3rd Semester Examination****PHYSICS****PAPER—PHS-301***Full Marks : 40**Time : 2 Hours**The figures in the margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable.**Illustrate the answers wherever necessary.****Use separate Answer-scripts for Group-A & Group-B*****Group-A**

[Marks : 20]

Answer Q. No. 1 & 2 and any one from the rest.

1. Answer any *three* bits : 2×3
- (a) Distinguish between adiabatic and sudden approximation.
- (b) What are the suitable conditions for the study of scattering problems by the method of partial waves ?
- (c) Explain Laporte selection rule.

(Turn Over)

- (d) In context of the He atom plot probability density for Fermi hole and Fermi heap.
- (e) 3 non-interacting bosons are trapped in an infinite potential well. Find the ground state energy.

2. Answer any one bit :

4

(a) If $\hat{H} = -\gamma \vec{S} \cdot \vec{B}$ where

$\vec{B} = B_0 \hat{z} + \hat{x} B_1 \cos \omega t - \hat{y} B_1 \sin \omega t$ is applied on an electron.

Derive the time dependent equation of motion for two level state.

(b) At what neutron lab energy will p-wave be important in n-p scattering ?

3. (a) In case of scattering from a spherically symmetric charge distribution the form factor is given by

$$F(q^2) = \int_0^{\infty} \rho(r) \frac{\sin\left(\frac{qr}{\hbar}\right)}{\left(\frac{qr}{\hbar}\right)} 4\pi r^2 dr$$

where $\rho(r)$ is the normalized charge distribution.

- (i) If the charge distribution of proton is approximately $\rho(r) = Ae^{-r/a}$, where A is a constant and 'a' is some characteristic radius of the proton. Show that form

factor is proportional to $\left(1 + \frac{q^2}{q_0^2}\right)^{-2}$ where q_0 is $\frac{h}{a}$.

- (ii) If $q_0^2 = 0.71 \left(\frac{\text{Gev}}{e}\right)^2$, find the characteristic radius of the proton.

- (b) Suppose one particle is a state $\psi_a(\mathbf{x})$ and the other is in $\psi_b(\mathbf{x})$. These two states are orthogonal and normalized. If the two particles are distinguishable, the combined wave function is $\psi_d(\mathbf{x}_1, \mathbf{x}_2)$. Calculate $\left\langle (\mathbf{x}_1 - \mathbf{x}_2)^2 \right\rangle_d$ for distinguishable particles and identical bosons.

4+3+3

4. (a) A one dimensional infinite potential well of width 'a' contains two spinless particles, each of mass m . The potential representing the interaction between the particles $V = A \delta(\mathbf{x}_1 - \mathbf{x}_2)$. Calculate the ground state energy of the system of the first order in A .
- (b) Obtain the zeroth-order wave function for the atom in the excited state $1S2p$.

5+5

Group-B

[Marks : 20]

Answer Q. No. 1 and any one from the rest.

1. Answer any five bits :

2×5

- (a) An ensemble of N three level systems with energies $\varepsilon = -\varepsilon_0, 0, +\varepsilon$ is in thermal equilibrium at temperature T . Find the free energy of the system at high temperature.
- (b) A system of N particles is enclosed in a volume V at a temperature T . The logarithmic of the partition function is given by $\ln Z = N \ln \left[(V - bN) (k_B T)^{3/2} \right]$ where b is a constant. Find the internal energy of the gas.
- (c) The equation of state of a real gas at moderate pressure is $P(V - b) = RT$; where R and b are constants. Find the partition function of the system.
- (d) Calculate the chemical potential of a system of N quantum harmonia oscillator having frequency w at temperature T .
- (e) Plot the temperature variation of chemical potential of B.E and F.D system of particles.
- (f) Prove that magnetic susceptibility of a system obeying classical mechanics and classical statistics is strictly equal to zero.

- (g) A two dimensional vector \vec{A} of given length $A = |\vec{A}|$ is equally likely to point in any direction specified by the angle θ from the x-axis. Find $\langle A_x \rangle$.

2. (a) In a uniform magnetic field B taken along z direction, the energy level of an electron is given by

$$E(l, p_z) = \hbar w_c \left(l + \frac{1}{2} \right) + \frac{p_z^2}{2m}$$

where $l = 0, 1, 2, \dots, \infty$ and $w_c = \frac{eB}{mc}$.

- (i) Find the degeneracy of the energy level.
- (ii) Calculate the partition function of the system.
- (iii) Show the magnetization at high temperature

$$M = -\mu_B \lambda \left(\frac{\mu_B B}{k_B T} \right).$$

where λ is the Langevin function.

- (b) Show that energy fluctuation in a canonical distribution is given by

$$\langle (E - \bar{E})^2 \rangle = k_B T^2 C_v. \quad 2+3+2+3$$

3. (a) Prove that pure state remains pure always.
- (b) Calculate the average value of q^2 for a quantum oscillator as function of T .

$$\hat{H} = -\frac{\hbar^2}{2m} \frac{d^2}{dq^2} + \frac{1}{2} m\omega^2 \hat{q}^2$$

Determine and explain the limiting values of $\langle q^2 \rangle$ for

$$\frac{k_B T}{\hbar\omega} \gg 1 \text{ and } \frac{k_B T}{\hbar\omega} \ll 1.$$

$$\text{Given : } \langle q | e^{-\beta \hat{H}} | q' \rangle = \left[\frac{m\omega}{2\pi\hbar \sinh(\beta\hbar\omega)} \right]^{1/2} \times$$

$$\exp \left[\frac{-m\omega}{4\hbar} \left\{ (q+q')^2 \tanh\left(\frac{\beta\hbar\omega}{2}\right) + (q-q')^2 \coth\left(\frac{\beta\hbar\omega}{2}\right) \right\} \right].$$

2+4+4