### 2017

# M.Sc. 2nd Semester Examination APPLIED MATHEMATICS WITH OCEANOLOGY AND COMPUTER PROGRAMMING

### PAPER-MTM-201

Full Marks: 50

Time: 2 Hours

The figures in the margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

Illustrate the answers wherever necessary.

## (Fluid Mechanics)

Answer Q. No. 1 and any four from the rest.

# 1. Answer any four questions:

4×2

- (a) Describe one, two and three-dimensional flows.
- (b) Discuss the similarity and dissimilarity between the vorticity and energy equations.

- (c) Write equations for inside and outside of the boundary layer for a flat plate at angle of attack of zero incidence in 2D steady, incompressible flow without effects of gravity.
- (d) Draw an infintesmally small moving element and show all energy fluxes along x-direction associated with the above element.
- (e) Define vortex line and vortex tube.
- (f) Write the expression for stream function for a uniform flow past a circular cylinder and hence draw stream lines around and inside the cylinder.
- 2. (a) Write the continuity equation for incompressible and viscous fluid flow in four forms: Integral-Conservation, Integral-Nonconservation, Differential-Conservation and Differential-Nonconservation.
  - (b) By some simplification, show that all above four forms of the continuity equation are equivalent to each other.

2+6

3. Draw infinitesimally small moving fluid element and show the forces in the z-direction for derivation of the z-component of the Navier-Stokes equation.

Finally derive the z-component of the Navier-Stokes equation in non-conservative form. 3+5

- 4. Consider steady, laminar, fully developed flow between two parallel plates separated by a distance 2H. The fluid is driven between the plates by an applied pressure gradient in the x-direction. It is assumed that the conduction in the y-direction is much greater than the conduction in x-direction.
  - (a) Determine the fully developed velocity distribution of the fluid as a function of the mean velocity.
  - (b) Determine the fully developed temperature distribution as a function of the surface and mean temperatures.

5+3

5. Write the Navier-Stokes equation in vector form and energy equation for Newtonian, imcompressible, viscous fluid flow with negligible gravity and radiation effects.

Make the above equations in non-dimensional form (Navier-Stokes equation in terms of Reynolds number  $Re = \frac{UL}{\gamma}$ , and energy equation in terms of Re and Prandtl number  $Pr = \frac{V}{\alpha}$ ) with the help of characteristics length,

velocity, pressure and temperature as L, U,  $rU^2$  and  $(T_W - T_C)$  respectively, where symbols have their usual meaning.

6. State and prove the Kelvin's theorem for barotropic fluid.

1+7

- (a) Define the rectilinear vortex and then find the complex
  potential due to a vortex of strength k placed at a point
  z<sub>0</sub>.
  - (b) State and prove the Blasius' Theorem. 4+4

[Internal Assessment -- 10]