

**2012****M.Sc.****1st Semester Examination****DISCRETE STRUCTURE****PAPER—COS-101**

Full Marks : 50

Time : 2 Hours

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words as far as practicable.*

*Illustrate the answers wherever necessary.*

*All notations have their usual meaning.*

**Module—1****(Set Theory)****(Marks : 25)**

Answer Q. No. 1 and any four from the rest.

1. Answer any two questions : 2+2
- (a) Define partition of a set. Explain it with an example. 1+1
- (b) Let  $n$  and  $k$  be positive integers with  $n \geq k$ . Then

$$\binom{n+1}{k} = \binom{n}{k-1} + \binom{n}{k}. \quad 2$$

(c) State Pigeonhole principle. How many students must be in a class to guarantee that at least two students received the same score on the final exam, if the exam is graded on a scale from 0 to 10 points. 1+1

2. Let A and B be subsets of a universal set U. Show that  $(A \cup B)' = A' \cap B'$  4

3. State the induction principle. If n be a positive integer then prove that

$$1^3 + 2^3 + \dots + n^3 = \left\{ \frac{n(n+1)}{2} \right\}^2 \quad 1+3$$

4. Suppose there are 10 members in a club.

(i) How many way can we select 5 members to stand in line for a picture ?

(ii) How many way can we select to make a 5 members committee ? 2+2

5. (i) How many bit string of length eight either start with a '0' bit or end with '1' bits.

(ii) A particular brand of shirt comes in 8 colours, has a male version and female version and comes in three sizes for each sex. How many different types of this shirt are made ? 2+2

6. If A, B, C be subsets of a universal set U. Prove that  $(A \cap B) \cup (B \cap C) \cup (C \cap A) = (A \cup B) \cap (B \cup C) \cap (C \cup A)$ . 4

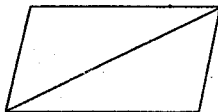
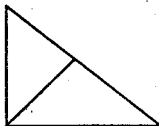
7. Among the first 100 positive integers, determine the integers which are divisible by 2 and 3, not by 5. 4

**[ Internal Assessment — 5 marks ]**

**Module—2**  
**(Graph Theory)**  
**(Marks : 25)**

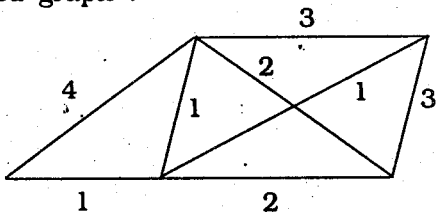
Answer any two questions : 2×10

1. (a) Define component of a graph. How many edges are there in a forest with  $n$  vertices and  $k$  components. 1+4
- (b) Define simple graph. What is the maximum number of edges in a simple graph with  $n$  vertices. 1+4
2. (a) Define isomorphic between two graphs. Show that following graphs are isomorphic :



- (b) Define walk, trail, path and cycle. Explain it with taking an example. 5
3. (a) Define Eulerian graph. For which value of  $n$ ,  $K_n$  (complete graph of  $n$  vertices) is Eulerian and why? 5
- (b) Define tree. Show that a circuit free graph with  $n$  vertices and  $(n - 1)$  edges is a tree. 5

4. (a) Define Eccentricity, center of a graph. Show that every tree has either one or two center. 5
- (b) Demonstrate the prim's algorithm of the following weighted graph :



**[Internal Assessment — 05]**

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